A MODEL FOR PASSIVE DISPERSION OF GAS AND PARTICLES

DISGAS-2.1

User Manual

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DISGAS is a 3-D time-dependent Eulerian model for transport of gas in the atmospheric surface layer.

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Abstract

The code DISGAS (model for passive DISpersion of GASes) is a Eulerian model for passive dispersion of diluted gas and fine dust particles. Turbulent diffusion is based on the K-theory and the wind field can be evaluated assuming either a uniform wind profile based on the Similarity Theory or using a terrain-following mass-consistent wind model. DISGAS can be used to forecast concentration of gas (or dust) over complex terrains. The inputs to the model are topography, wind observations from meteorological stations, atmospheric stability information, and gas flow rate from a discrete number of point sources. DISGAS is written in fortran 90. Here we describe the model and an application example.

1 Introduction

Several volcanic and non-volcanic sources in central Italy and worldwide emit a large amount of gas, such as carbon dioxide (CO_2) and other components, through focused or diffuse degassing, producing consistent gas plumes that are dispersed in the lower part of the atmosphere (e.g., Chiodini et al., 2005; Costa et al., 2005; Chiodini et al., 2007).

The cloud dispersion of a gas denser than air released from a given source, is governed by the gravity and by the effects of lateral eddies which increase the mixing with air around the edges of the plume, decreasing its density. In the initial phase the negative buoyancy controls the gas dispersion and the cloud follows the ground (gravitational phase). During this phase, the dispersion of heavy gas is markedly different from passive gas dispersion (and even from positively buoyant gas). When density contrast is not important, gas dispersion is basically governed by wind and atmospheric turbulence (passive dispersion).

From a theoretical point of view, dispersion of natural gases can be fully studied by solving the complete equations for mass, momentum, and energy transport. However, in actual practice, different simplified approaches able to describe only specific phases or aspects of gas transport are commonly used. The most general and computationally most expensive models are given by three-dimensional CFD models based on the transport theory of mass, momentum, energy, and species (e.g., Macedonio and Costa, 2002; Cortis and Oldenburg, 2009; Cerminara et al., 2016). This approach is able to simulate dispersion of both heavy and light gases accounting for topographic effects, variation of atmospheric conditions and wind direction, etc.

For a gas denser than air the shallow layer approach, which uses depth-averaged variables to describe the flow behaviour, is commonly used (e.g., Hankin and Britter, 1999; Costa et al., 2008; Folch et al., 2009). Models based on this approach are applied to describe gravity driven flows of dense gas over complex topography (Costa et al., 2008; Chiodini et al., 2010).

For dispersion of a diluted gas, which is passively driven by wind advection and atmospheric turbulence, simpler advection-diffusion equations can be solved (e.g., Prabha and Mursch-Radlgruber, 1999a), like in the model we describe here. DISGAS (Costa and Macedonio, 2016) is based on an explicit solver of the advection-diffusion equation which uses a second-order Lax-Wendroff scheme (e.g., Ewing and Wang, 2001) and can be coupled with a wind profile described by the similarity theory (De Bruin et al., 2000) or with a mass-consistent wind model (Douglas and Kessler, 1990).

The generalization of the advection-diffusion equation including a sedimentation term, allows the model to be applied to study even the dispersion of a diluted mixture of very fine particles into the atmospheric surface layer. For instance, with such a generalization the model can describe the dispersion of small fibres like asbestos or small powders like pollen.

Here, firstly we summarize the theory and equations on which the model is based, then we illustrate the numerical method used to solve the equations, and, in the Appendix A, we describe the program setup, folder structure, input/output files, and how to run the code. Simulation results obtained for the dispersal of CO_2 emitted from the Solfatara crater in the Campi Flegrei, in surroundings areas of the he city of Naples, Italy, is also presented as an example of application (Granieri et al., 2013). The format and the description of input and output files is reported in the Appendix B and Appendix C.

2 Physical model

A full description of gas dispersion into the atmosphere requires the solution of mass, momentum, energy and species transport equations (see *e.g.* Macedonio and Costa, 2002). This implies a relatively high computational effort and sometimes it is impossible to study the gas dispersion in complex large domains, especially in the surface layer where a large range of length scales are involved.

In order to reduce the computational time we introduce some assumptions. Our main objective is to solve the advection-diffusion equation for the gas concentration $c = \langle c \rangle + c'$:

$$\frac{\partial \langle c \rangle}{\partial t} + \frac{\partial u_x \langle c \rangle}{\partial x} + \frac{\partial u_y \langle c \rangle}{\partial y} + \frac{\partial u_z \langle c \rangle}{\partial z} + \frac{\partial \langle u'_x c' \rangle}{\partial x} + \frac{\partial \langle u'_y c' \rangle}{\partial y} + \frac{\partial \langle u'_z c' \rangle}{\partial z} = \langle Q \rangle \tag{1}$$

where $\mathbf{V} = (u_x + u'_x, u_y + u'_y, u_z + u'_z)$ is the wind field and $\langle Q \rangle$ is a source term, i.e. the gas mass flux from the ground. Plain terms in lower case letters represent the average part, terms with the symbol prime ' their turbulent fluctuations and the overbar defines the filtering operation on the product of the fluctuation terms (e.g., Sagaut, 2006).

Hence, as in other studies (e.g., Prabha and Mursch-Radlgruber, 1999a,b; Costa et al., 2005), we do not solve the complete set of the coupled equations for mass, momentum, energy, and concentration, but we solve eq. (1) and approximate the wind field as given by a uniform profile (for relatively small domains) or estimate it using a diagnostic wind model which produces a zero three-dimensional divergence velocity field consistent with the measured values, avoiding artificial generation or loss of gas. Turbulent terms are parameterized according with the K-theory as described later. The passive dispersion approach can be used when the gas is diluted enough, and the validity of such an approximation can be assessed by estimating the Richardson number (e.g., Britter and McQuaid, 1988; Cortis and Oldenburg, 2009; Costa et al., 2013):

$$R_i = \frac{(g'q)^{2/3}}{V^2 R^{2/3}} \tag{2}$$

where $g' = (g(\rho_g - \rho_a))/\rho_a$ is the reduced gravity acceleration (being g the gravity acceleration, ρ_a and ρ_g the air and the gas density respectively), q is the volumetric flow rate, R the plume size (e.g. plume radius), and V is the wind velocity at the reference altitude (i.e., 10 m). For $R_i < 0.25$ transport is substantially passive whereas for $R_i > 1$ is mainly density driven (Cortis and Oldenburg, 2009; Costa et al., 2013).

2.1 Wind field

For evaluating the wind field there are two options:

1. The simplest choice (SIMILARITY) consists of assuming a horizontally uniform wind profile calculated in accord to the wind measurements and the Monin-Obukhov similarity theory (Monin and Yaglom, 1979; Byun, 1990):

$$u(z) = \frac{u_*}{k} \left[\ln(z/z_0) - \Psi_m(z/L) \right]$$
(3)

where k = 0.4 is the von Karman constant, z_0 is the roughness length, u_* the friction velocity and $\Psi_m(x)$ the atmospheric stability function for the momentum (see *e.g.* Dyer, 1974; Jacobson, 1999). The friction velocity can be calculated as:

$$\frac{u_*}{k} = \frac{u(z_1)}{\ln(z_1/z_0) - \Psi_m(z_1/L) + \Psi_m(z_0/L)}$$
(4)

where z_1 is the height at which the wind velocity $u(z_1)$ is known. Roughness can be assumed uniform or given as a matrix covering the computational domain. Using the SIMILARITY option implies the wind can be not mass-consistent (e.g. $\nabla \cdot V$ can be locally not null). It is adequate for flat small domains but is not suitable for large domain and complex terrains.

2. Another choice (DIAGNO) consists of using the wind field estimated by the Diagnostic Wind Model (DWM), a model developed by the United States Environmental Protection Agency (EPA), here named DIAGNO. This model generates the wind components (U, V, W) in a terrain following coordinates system.

The DIAGNO needs topographic data, average wind on the computational domain and atmospheric stability information within the scale of the domain (the temperature gradient dT/dz).

In a first step the domain-mean wind is adjusted for the kinematic effects of terrain (lifting and acceleration of the airflow over terrain obstacles), thermodynamically generated slope flows, and blocking effects.

In a second step, wind observations, when available, are added to the first step field, and an objective analysis scheme is used to produce a new gridded field (U, V, W). The scheme is designed so that the observations are used to define the wind field within a user-specified radius of influence while the first step (U, V, W) field is used in subregions in which observations are unavailable.

Finally, a divergence-minimization procedure in terrain following coordinates is iteratively applied until the inequality:

$$\nabla \cdot \mathbf{U} < \epsilon \tag{5}$$

is satisfied ($\mathbf{U} = (U, V, W)$) and ϵ is an arbitrarily user defined small number). The final product of DWM is an approximately null-divergence wind field consistent with the observations (for further information see Douglas and Kessler, 1990).

The approximation of null-divergence wind field is generally applicable up to a kilometer above ground level (Dutton and Fichtl, 1969) therefore to our study, since we treat the surface layer, *i.e.* the lowest part of the Planetary Boundary Layer (PBL).

Since terrain-following coordinate are used such an approximation still holds even if ground level varies significantly within the computational domain. DISGAS model interpolates the wind field into its computational grid.

2.2 Turbulence parameterization

Turbulent fluxes are given by the product of the fluctuation terms, and in agreement with the "K-theory", they are expressed in terms of gradients of average concentration:

$$\langle u'_x c' \rangle = -K_x \frac{\partial}{\partial x} \langle c \rangle \qquad \langle u'_y c' \rangle = -K_y \frac{\partial}{\partial y} \langle c \rangle \qquad \langle u'_z c' \rangle = -K_z \frac{\partial}{\partial z} \langle c \rangle \tag{6}$$

where $K = (K_x, K_y, K_z)$ is the turbulent diagonal diffusivity tensor.

Inside the atmospheric surface layer, the Monin-Obukhov similarity theory allows to estimate the vertical turbulent diffusivity K_z in terms of friction velocity u_* and the Monin-Obukhov length L:

$$K_z = \frac{\kappa z u_*}{\phi_h} \tag{7}$$

where κ is the von Karman constant ($\kappa = 0.4$), z is the distance from the ground and ϕ_h is the atmospheric stability function for temperature (see Jacobson, 1999):

$$\phi_{h} = \begin{cases} Pr_{t} + \beta_{h} \frac{z}{L} & z/L > 0 \text{ stable condition} \\ Pr_{t} \left(1 - \gamma_{h} \frac{z}{L}\right)^{-1/2} & z/L < 0 \text{ unstable condition} \\ Pr_{t} & z/L = 0 \text{ neutral condition} \end{cases}$$
(8)

with $\beta_h = 7.8$, $\gamma_h = 11.6$ and $Pr_t \approx 0.95$. Therefore, evaluating K_z requires knowledge of the friction velocity u_* and the Monin-Obukhov length L.

From a practical point of view, L is often a quantity difficult to directly estimate. Instead, it is operationally easier to evaluate this length using the "Bulk Richardson number" method (Golder, 1972):

$$Ri_b = \frac{g}{T} \frac{\partial \theta}{\partial z} \frac{z_m^2}{u_m^2} \tag{9}$$

where g is the gravity, θ and T the potential and the absolute air temperature (Jacobson, 1999), z_m the geometric mean thickness of the considered layer and u_m is the logarithmically interpolated wind speed at z_m . The Richardson number Ri is a measure of the dynamics on the buoyancy effects: we have atmospheric instability when $Ri_b < Ri_crit$ and stability for $Ri_b > Ri_crit$ ($Ri_crit \simeq 0.2$). The term z/L can be calculated analytically in terms of $R_i b$ by using the relationship (Byun, 1990):

$$\frac{z}{L} = Ri_b \frac{\phi_m^2}{\phi_h} \tag{10}$$

As explained in the Appendix B, Monin-Obukhov length L can be directly furnished by the user (if the option SONIC is used for the wind file) or estimated from air temperature difference following the "Bulk Richardson number" method (if the option CUP is used for the wind file). Concerning the horizontal eddy diffusivity, K_z and K_H can be assumed either approximated as constant or considered variable. In the latter case, following the large eddy approach (e.g., Smagorinsky, 1963; Pielke et al., 1992; Byun and Schere, 2006), the horizontal eddy diffusivity $K_x = K_y = K_H$ is considered isotropic and estimated as (Byun and Schere, 2006):

$$K_h = Pr_t \alpha^2 \Delta x \Delta y \sqrt{\left(\frac{\partial v_x}{\partial x} - \frac{\partial v_y}{\partial y}\right)^2 + \left(\frac{\partial v_y}{\partial x} + \frac{\partial v_x}{\partial y}\right)^2} \tag{11}$$

were $\alpha \simeq 0.28$ is a dimensionless constant empirically determined, and Δx and Δy the grid spacing (in DISGAS-2.1 we set $\alpha = 3$). A lower limit of $K_H = 0.075(\sqrt{\Delta x \Delta y})^{4/3} \text{ m}^2/\text{s}$ was imposed (Pielke et al., 1992). As we mentioned above, here we neglect the off-diagonal horizontal and vertical turbulent diffusion components (Toon et al., 1988; Jacobson et al., 1996; Park and Kim, 1999). For a more general treatment that includes the off-diagonal diffusion components see (Byun and Chin, 1999).

3 Numerical solution

Considering the assumptions introduced above and a null-divergence wind field, in a terrain-following coordinate system (Douglas and Kessler, 1990) consisting of:

$$X = x, \quad Y = y, \quad Z = z - h(x, y)$$
 (12)

being (h(x, y) the height of the topography, eq. (1) for the mean scaled concentration C may be re-written in a generalized form as (Toon et al., 1988; Jacobson et al., 1996; Costa, 2006):

$$\frac{\partial C}{\partial t} + U \frac{\partial C}{\partial x} + V \frac{\partial C}{\partial y} + W \frac{\partial C}{\partial z_*} =$$

$$\frac{\partial}{\partial x} \left(K_h \frac{\partial C}{\partial x} \right) + \frac{\partial}{\partial y} \left(K_h \frac{\partial C}{\partial y} \right) + \frac{\partial}{\partial z_*} \left(K_z \frac{\partial C}{\partial z_*} \right) + \langle Q_* \rangle$$
(13)

here (U, V, W) denote the scaled wind speeds, K_h and K_z are the diagonal scaled diffusion coefficients and Q_* the source term in the new coordinates. In the case of the simple transformations (12) the Jacobian is equal to the unit, $J = \partial z / \partial z_* = 1$, therefore $c(x, y, z) = C(x, y, z_*)$ and $Q = Q_*$. In the case of particle dispersion, here W represents the sum of the vertical wind component and of the particle settling velocity V_s , *i.e.* $W = V_{Z,Wind} - V_s$.

The advective terms are discretised according to the Lax-Wendroff scheme which is second-order (see e.g. Ewing and Wang, 2001). For instance, the advective term in the X-direction yields:

$$-\Delta t \left(U \frac{\partial C}{\partial x} \right)_{i,j,k}^{n} = -\frac{Cr}{2} \left(C_{i+1,j,k}^{n} - C_{i-1,j,k}^{n} \right) + \frac{Cr^{2}}{2} \left(C_{i+1,j,k}^{n} - 2C_{i,j,k}^{n} + C_{i-1,j,k}^{n} \right)$$
(14)

where $Cr = U\Delta t/\Delta x$ represents the Courant number (Δx is the grid spacing and Δt the computational time step). In order to reduce the numerical over- and under-shooting that commonly affects high-order schemes near discontinuities one can use slope limiter methods. In fact, these methods preserve the monotonicity of the solution while the accuracy remain higher than the first order upwind methods (Sweeby, 1984; Wang and Hutter, 2001; Ewing and Wang, 2001). For instance, applying the minmod slope-limiter method and considering the general case with non-uniform velocity, equation (14) becomes:

$$-\Delta t \left(U \frac{\partial C}{\partial X} \right)_{i,j,k}^{n} = -\frac{\Delta t}{\Delta x} \left(U_{i,j,k}^{n} C_{i,j,k}^{n} - U_{i-1,j,k}^{n} C_{i-1,j,k}^{n} \right) - \frac{\Delta x}{2} \left[Cr_{i,j,k}^{n} (1 - Cr_{i,j,k}^{n}) \sigma_{i,j,k}^{n} - Cr_{i-1,j,k}^{n} (1 - Cr_{i-1,j,k}^{n}) \sigma_{i-1,j,k}^{n} \right]$$
(15)

where $Cr_{i,j,k}^n = U_{i,j,k}^n \Delta t / \Delta x$, and:

$$\sigma_{i,j,k}^{n} = \operatorname{minmod}\left\{\frac{C_{i+1,j,k}^{n} - C_{i,j,k}^{n}}{\Delta x}, \frac{C_{i,j,k}^{n} - C_{i-1,j,k}^{n}}{\Delta x}\right\}$$
(16)

with minmod $(a, b) = 1/2(\operatorname{sgn}(a) + \operatorname{sgn}(b)) \min(|a|, |b|)$ (Ewing and Wang, 2001). The introduction of alternative limiter methods is straightforward.

The diffusion terms are evaluated using a central difference scheme for the general case with a not uniform turbulent diffusivity tensor, e.g. in the z-direction using:

$$\frac{\partial}{\partial x} \left(K_h \frac{\partial C}{\partial x} \right) = \frac{1}{2\Delta x^2} \left[\left(K_h^{i,j,k} + K_h^{i-1,j,k} \right) C_{i-1,j,k} - \left(K_h^{i+1,j,k} + 2K_h^{i,j,k} + K_h^{i-1,j,k} \right) C_{i,j,k} + \left(K_h^{i+1,j,k} + K_h^{i,j,k} \right) C_{i+1,j,k} \right]$$
(17)

The stability of the numerical scheme is ensured by using a time step Δt lower than the critical. As established by Hindmarsh et al. (1984), an explicit scheme for the multidimensional advection diffusion equation is numerically stable if the condition:

$$\Delta t \le \frac{1}{\left[2\left(\frac{K_h}{\Delta x^2} + \frac{K_h}{\Delta y^2} + \frac{K_z}{\Delta z_*^2}\right) + \frac{U}{\Delta x} + \frac{V}{\Delta y} + \frac{W}{\Delta z_*}\right]}$$
(18)

Concerning the z-direction, the numerical scheme was generalized to a non-uniform vertical grid.

4 Application example

DISGAS code was applied to simulate gas dispersion from the Solfatara volcano, Campi Flegrei, Italy (Granieri et al., 2013). Solfatara releases more than 1000 t d⁻¹ of CO₂ through soil diffuse degassing from a relatively small area (0.5-1 km²) (Chiodini et al., 2001; Granieri et al., 2013). Temperature of the gases emitted from Solfatara area is relatively high: fumaroles temperature is between 96 °C and 162 °C (Chiodini et al., 2001) and, flux weighted temperature of diffusing soil is 66 °C (Costa et al., 2005).

This implies a density decrease due to temperature that almost balances the increase due to the greater molecular weight directly at the source $(M_{CO_2}/M_{air} = 44/29 \text{ while } T_{CO_2}/T_{air} \approx 400/300)$. Moreover low wind conditions are rarely recorded at Solfatara (daily average wind intensity U > 1 m/s is about 75% of the total and the cases with U < 0.1 m/s 0.05% of the total). For these reasons, the passive dispersion assumption, described in Section 2, is appropriate (Costa et al., 2005; Granieri et al., 2013).

Simulation results of gas dispersal were first compared with observations, then the model was used to investigate space and time evolution of the volcanic CO_2 plume under different meteorological conditions in order to assess its potential hazard.

Using DISGAS, Granieri et al. (2013) showed that the urban area of Naples is mantled by the volcanic plume of the Solfatara when atmospheric circulatory patterns are dominated by the locally frequent marine winds. In these conditions the air CO_2 content increases above the normal air CO_2 content, with

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differences varying from more than one thousand ppm (above the normal atmospheric background) in proximity of the Solfatara crater to a few ten ppm at a few kilometres from the source. Although these values indicate that there is no risk to the population, the elevated CO_2 concentration contributes to the deterioration of air quality in Naples, especially on days with atmospheric stagnant conditions.

An emission rate five times higher than the current one may pose a hazard even for the human health. In Figure 1 we reported some simulation results of Granieri et al. (2013). Simulations of typical CO_2 concentrations at 1.5 m of height (typical breathing level for humans) suggest that CO_2 concentration reaches higher values during nocturnal hours (from 2:00 to 7:00), when atmosphere is very stable. The level goes down up to a few hundred ppm at a few km from the source. During daytime, with unstable conditions and more intense wind circulation, gas is diluted and typical concentration values range from a few hundreds ppm near the source up to a few tens ppm (above the normal atmospheric background) at 3-4 km from the source (for further details see Granieri et al., 2013).



Figure 1: Average CO_2 concentration maps at 1.5 m above ground level assuming the mean CO_2 emission rate of 1067 ton/d (figures a and b on the top) and the maximum CO_2 emission rate measured in the 1998-2008 period of 1800 ton/d (figures c and d on the bottom), over a whole diurnal cycle (figures a and c) and over nocturnal periods (figures b and d). Modified after Granieri et al. (2013).

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Appendix A Program setup

Here we will describe how to install DISGAS model and the code structure.

A.1 Installation

- On a Unix/Linux/Mac X operating system:
 - 1. Uncompress and untar file disgas-2.1.tar.gz with the commands:

tar xzvf disgas-2.1.tar.gz

This will generate directory disgas-2.1 and the folder structure described in the Figure 2.

- 2. Configure, compile and install the program disgas and the utility (grd2lw). Enter the directory disgas-2.1, then issue the command configure, and make install.
 - After the command make install, the generated executable files disgas and grd2lw will be installed in the directory \$HOME/bin (the directory bin under the home directory will be automatically created if needed). It is important that the directory \$HOME/bin is in the PATH of your shell. After compilation you may issue the command make clean to remove unneeded files.

Please note that since disgas-2.1, the utility diagno is distributed separately. This version is compatible with diagno-1.1.1.

A.2 Folder structure

Figure 2 shows the folder structure of DISGAS-2.1. When untarred, disgas-2.1.tar.gz generates a directory tree as shown in Figure 2. The directory disgas-2.1/src contains the source code of DISGAS n FORTRAN-90 whereas directory bin is automatically generated during the installation process and contains the executable binaries. The source codes of the provided utilities are contained under disgas-2.1/utils. The directory disgas-2.1/examples contains two subdirectories example1 and example2 with examples of applications of DISGAS, which can be used to test the installation.

Example 1 adopts a uniform wind (SIMILARITY flag in disgas.inp), whereas example 2 adopts a wind generated by program diagno. Please, note that since DISGAS-2.1 diagno is distributed separately. Further details on how to run the examples are contained in file example/README. The directory outfiles where the output files are generated is automatically created by disgas (if non existent). The pathname of the output directory is defined in the input file of disgas. Finally, the doc directory contains the documentation of DISGAS (this file).

A.3 Program run

For running the example of disgas-2.1 you need to previously install diagno-1.1.1, which provides the utilities presfc and diagno.

Then, programs presfc, diagno and disgas can be launched typing, respectively,

- presfc
- diagno
- disgas problemname.inp



Figure 2: Directory tree of disgas-2.1.

where problemname.inp is the name of the control input file (see Appendix B). The file diagno.inp denotes the DIAGNO input file. Beside diagno.inp for running DIAGNO (distributed separately), it is necessary to furnish, in the same directory, a file surface.dat containing data from wind stations and a topography file topography.grd. The file surface.dat can be generated using the utility PRESFC that needs the input file presfc.dat (for further descriptions see Douglas and Kessler, 1990). The DIAGNO computational domain has to be equal or larger than the DISGAS computational domain. NOTE: To create a new run simply create a new folder in the directory examples (with subfolder outfiles), copy the input files and the problemname.inp. <u>NOTE</u>: To create a new run simply create a new folder in the directory examples (with subfolder outfiles), copy and edit the input files.

Appendix B The DISGAS input and output files

DISGAS needs of the following input files:

- File: problemname.inp Control file that defines a run. Mandatory.
- File: topography.grd Regional ground elevation file. Optional.
- File: source.dat Source term (gas fluxes) file. Mandatory.
- File: winds.dat Meteorological data file. Optional.
- File: diagno.out DIAGNO meteorological data file. Optional.

<u>NOTE</u>: File names used in this manual are given just for illustrative purposes. Names and paths of input files are absolutely free and can be defined by the user in the control file problemname.inp.

B.1 The control file problemname.inp

The DISGAS control file is passed to the program as a call argument. This file is made up with a set of blocks that define all the computational and physical parameters needed by the dispersion model (Table 1 shows an example of control file). Parameters within a block are listed one per record, in arbitrary order, and can optionally be followed by one or more blank spaces and a comment. A detailed description of each record is given below. Real numbers can be expressed following the FORTRAN notation (*e.g.*: $12e7 = 12 \times 10^7$).

B.1.1 BLOCK TIME

- YEAR: Initial year.
- MONTH: Initial month (1-12).

- DAY: Initial day (1-31).
- HOUR: Initial hour (0-23).
- MINUTE: Initial minute (0-59).
- SIMULATION_INTERVAL_(SEC): Simulation time duration (in seconds).
- RESTART_RUN: Select whether the simulation loads the restart file (NO or YES).
- RESET_TIME: In case of start from the restart file, select whether the internal variable time is reset to zero or continues from last dump. This affects also the reset or the continuation of the numeration of the output files (NO or YES).

<u>NOTE</u>: The parameters YEAR, MONTH, DAY, HOUR, and MINUTE are used to check the consistence with both the restart and the meteorological files.

B.1.2 BLOCK GRID

- NX: Number of grid cells along the *x*-direction.
- NY: Number of grid cells along the *y*-direction.
- NZ: Number of layers along the z-direction.
- Z_LAYERS_(M): List of the quotes of the layers in the z-direction. They must be exactly NZ.
- DX_(M): Grid spacing along the *x*-direction (in meters).
- DY_(M): Grid spacing along the *y*-direction (in meters).
- X_ORIGIN_(UTM_M): x-coordinate of the grid bottom left corner (UTM coordinates in meters).
- Y_ORIGIN_(UTM_M): y-coordinate of the grid bottom left corner (UTM coordinates in meters).

B.1.3 BLOCK PROPERTIES

- DISPERSION_TYPE: Type of material dispersed. Possibilities are GAS (no settling velocity) or PARTICLES (settling velocity is calculated in accord to the particle properties specified below).
- PARTICLE_DIAMETER: Diameter of particles in metres (only used if DISPERSION_TYPE=PARTICLES).
- PARTICLE_DENSITY: Density of particles in kg/m³ (only used if DISPERSION_TYPE=PARTICLES).
- PARTICLE_SHAPE_PARAMETER: Particle shape parameter to be used to calculated particle settling velocity, *i.e.* particle sphericity or particle aspect ratio. In the case of Ganser (1993) model it corresponds to particle sphericity (only used if DISPERSION_TYPE=PARTICLES). PARTICLE_MODEL_VSET: Parameterization used for calculating particle settling velocity. Possibilities are: ARASTOOPOUR for the Arastoopour et al. (1982) model (spherical particles), GANSER for Ganser (1993) model, WILSON_HUANG for Wilson and Huang (1979) model (only used if DISPERSION_TYPE=PARTICLES).

B.1.4 BLOCK TOPOGRAPHY

- EXTRACT_TOPOGRAPHY_FROM_FILE: Flag indicating whether the topography of the computational domain is extracted from a ground elevation file or not. Possibilities are YES/NO. If YES, topography is extracted from the file defined in the FILES BLOCK. If NO, a flat terrain is assumed with slopes in the x and y directions defined by the parameters X_SLOPE_(DEG) and Y_SLOPE_(DEG).
- Z_ORIGIN_(M): Quote of the bottom-left corner of the topography. This is used to generate a flat topography when the flag EXTRACT_TOPOGRAPHY_FROM_FILE is set to NO.

- X_SLOPE_(DEG): Slope of the flat topography in the x direction (in degrees). This parameter is used to generate a flat topography when the flag EXTRACT_TOPOGRAPHY_FROM_FILE is set to NO.
- Y_SLOPE_(DEG): Slope of the flat topography in the y direction (in degrees). This parameter is used to generate a flat topography when the flag EXTRACT_TOPOGRAPHY_FROM_FILE is set to NO.

B.1.5 BLOCK METEO

- WIND_MODEL: Flag indicating the wind model. Possibilities are SIMILARITY or DIAGNO. If SIMILARITY is set, the wind (horizontally uniform) is read from a wind file defined in the BLOCK FILES, and the vertical profile is evaluated according to the similarity theory. If DIAGNO, meteorological data (variable in both space and time) is read from a DIAGNO output file defined in the FILES BLOCK. Note that in the later case the program DIAGNO must necessarily run before the program DISGAS and parameters read from the file winds.dat are used as input for DIAGNO (see Sec. 2.1).
- HORIZONTAL_TURB_MODEL: Flag indicating the model for the horizontal diffusion coefficients. This may be equal to CONSTANT for constant horizontal diffusion coefficients or SMAGORINSKY for horizontal diffusion coefficient from the Smagorinsky model (see eq. (11)).
- VERTICAL_TURB_MODEL: Flag indicating the model for the vertical diffusion coefficient. This may be set to 0 (zero) for constant vertical diffusion coefficient or 1 (one) for vertical diffusion coefficient from Atmospheric Boundary Level (ABL) model (see eq. (7)).
- ROUGHNESS_MODEL: Flag indicating the soil roughness length model. Possibilities are UNIFORM (set with the parameter ROUGHNESS_LENGTH) or MATRIX for non-uniform roughness length, provided with a file (see BLOCK FILES).
- ROUGHNESS_LENGTH: Terrain roughness height z_o (in m). The surface roughness height is related to the vertical wind profile. Values range from about 10^{-5} m over an iced surface, 0.005 m over naked soil, 0.05 m over soil covered by tall grass, or up to 1 m or more over forest or urban areas.
- DIFF_COEFF_HORIZONTAL: Horizontal diffusion coefficient in m²/s, used if HORIZONTAL_TURB_MODEL is equal to CONSTANT.
- DIFF_COEFF_VERTICAL: Vertical diffusion coefficient in m²/s, used if VERTICAL_TURB_MODEL is equal to CONSTANT.

B.1.6 BLOCK FILES

- TOPOGRAPHY_FILE_PATH: Name (including relative or absolute path) of the topography file. See Sec. B.2 for file format details. This record is read only when EXTRACT_TOPOGRAPHY_FROM_FILE = YES.
- ROUGHNESS_FILE_PATH: Name (including relative or absolute path) of the file containing the roughness. See Sec. B.4 for file format details. This record is read only when ROUGHNESS_MODEL = MATRIX.
- RESTART_FILE_PATH: Name (including relative or absolute path) of the restart file. This file is automatically generated and overwritten by **disgas** at every print time. It may be later used to restart the simulation from the last dump. See Sec. B.1.1 and B.9.
- SOURCE_FILE_PATH: Name (including relative or absolute path) of the source file. See section B.3 for file format details.
- WIND_FILE_PATH: Name (including relative or absolute path) of the wind data file. See section B.5 for file format details.
- DIAGNO_FILE_PATH: Name (including relative or absolute path) of the DIAGNO output file. This is a binary unformatted file created by DIAGNO. Only used when WIND_MODEL = DIAGNO.

• OUTPUT_DIRECTORY: Name (including relative or absolute path) of the folder where DISGAS output files are written.

B.1.7 BLOCK OUTPUT

- LOG_VERBOSITY_LEVEL: Flag indicating verbosity level of the log file. Possibilities are 0, for low verbosity log file, and 1, for high verbosity log file.
- OUTPUT_GRD_TYPE: Format for the GRD file. Possibilities are ASCII or BINARY (in the current version ASCII only).
- OUTPUT_INTERVAL_(SEC): Time interval to output results (in s).
- OUTPUT_U_VELOCITY: Flag indicating whether the wind velocity in the x direction (in m/s) has to be printed or not. Possibilities are YES or NO. If YES, a GRD-format file for each height is dumped in the folder defined by the OUTPUT_DIRECTORY recorded every OUTPUT_INTERVAL_(SEC) seconds.
- OUTPUT_V_VELOCITY: Flag indicating whether the wind velocity in the y direction (in m/s) has to be printed or not. Possibilities are YES or NO. If YES, a GRD-format file for each height is dumped in the folder defined by the OUTPUT_DIRECTORY recorded every OUTPUT_INTERVAL_(SEC) seconds.
- OUTPUT_CONCENTRATION: Flag indicating whether the gas concentration (in ppm) has to be printed or not. Possibilities are YES or NO. If YES, a GRD-format file for each height is dumped in the folder defined by the OUTPUT_DIRECTORY record every OUTPUT_INTERVAL_(SEC) seconds.
- OUTPUT_LAYER: Flag indicating the number of printed NZ layer. Possibilities are ALL or list of layers.
- TRACK_POINTS: Flag indicating the presence of tracking points. Possibilities are YES or NO.
- N_POINTS: Flag indicating the number of tracking points.
- POINTS_EASTING: Flag indicating the Easting coordinates (UTM) of tracking points.
- POINTS_NORTHING: Flag indicating the Northing coordinates (UTM) of tracking points.
- POINTS_ELEVATION: Flag indicating the elevation (m) of tracking points.

B.2 The topography file topography.grd

The topography file specifies ground elevation at a regional scale (*i.e.* in a region typically equal or larger than the computational domain). Topography must be specified on a structured grid using arbitrary (but constant) grid spacing (*e.g.*, 5 m, 10 m, 100 m, *etc.*). Discretizations along x- and y-directions (grid spacing) can be different. The only necessary requirement is that the computational domain must lay within the bounds of the region where topography is specified. DISGAS reads the topography file and automatically interpolates elevations onto the nodes of the computational grid. In this version of **disgas**, the topography must be stored in the ASCII GRD format. The structure of a GRD format file is described in Sec. C (see also Table 4).

B.3 The source file source.dat

The source file specifies the gas fluxes (mass flow rate expressed in kg/s) from different point sources. DISGAS reads this file and automatically locates the source onto the nearest node of the computational domain. In case multiple records are assigned the same node, the mass fluxes for that node are summed. Each concentrated point source is listed in the source file with the following record structure:

- X_s : x-coordinate (UTM in m) of the source.
- Y_s : y-coordinate (UTM in m) of the source.

• PHI_s: Flux associated to the point source, expressed in kg/s.

There is no limit to the number of point sources; point sources located outside the computational domain are automatically rejected.

B.4 The roughness length file roughness.grd

This file specifies the roughness-length in a region typically equal or larger than the computational domain. The roughness length (in m) must be specified on a structured grid using arbitrary (but constant) grid spacing (e.g., 5 m, 10 m, 100 m, etc.). Discretizations along x- and y-directions (grid spacing) can be different. The only necessary requirement is that the computational domain must lay within the bounds of the region where roughness length is specified. DISGAS reads this file and automatically interpolates the values onto the nodes of the computational grid. In this version of disgas, the roughness length must be stored in the ASCII GRD format. The structure of the roughness length file is the same as the topography.grd file, and is described in Sec. C (see also Table 4).

B.5 The wind data file winds.dat

The wind data file contains meteorological data at different time slices. If the record WIND_MODEL, in the control input file, is UNIFORM, DISGAS reads this wind file and estimates the Atmospheric Surface Layer parameters. Otherwise, if the record WIND_MODEL is DIAGNO, the wind field is instead read by the DIAGNO output file (file diagno.out). The wind file format is described in Table 2 (if code=CUP) and Table 3 (if code=SONIC) and the meaning of the used symbols is the following:

- X_UTM, Y_UTM : UTM coordinates of the wind station (specified in the first record of the file).
- Z_ref : Elevation above ground of the wind station (specified in the first record of the file).
- iyr : Measurement year.
- imo : Measurement month (1-12).
- idy : Measurement day (1-31).
- ihr : Measurement hour (0-23).
- imi : Measurement minute (0-59).
- code : Flag that indicates the type of anemometer. Possibilities are CUP or SONIC.
- t_1 : Time slice starting time (in s after initial time). Initial time for measurements is assumed to be at day idy, hour ihr, and minute imi.
- t_2 : Time slice ending time (in s after initial time). Initial time for measurements is assumed to be at day idy, hour ihr, and minute imi. A data time slice spans during the interval [t_1,t_2].
- wx : x-component of wind speed (in m/s).
- wy : y-component of wind speed (in m/s).
- T_z0 : Temperature (in ^oC) at the ground level.
- T_zref : Temperature (in ^oC), measured at Z_ref.
- p : Atmospheric pressure (in hPa).
- ustar : Friction velocity (in m/s).
- L : Monin-Obukhov length (in m).

<u>NOTE</u>: The records iyr to imi are used just to check consistency of meteorological data files with the input control file. Initial time must coincide in both cases.

B.6 The DIAGNO file diagno.out

The 3-D time-dependent wind field produced by the utility DIAGNO is stored in the unformatted file diagno.out. The format of this file is defined by subroutine outfil.f of diagno-1.1.1 distributed separately). This subroutine was modified with respect to the original contained in the utility diagno written by Douglas and Kessler (1990). The format of file diagno.out is not described here since it cannot be edited (see the user guide of diagno.

B.7 The DISGAS output files

At each user specified time (see $OUTPUT_INTERVAL(SEC)$ record in the control file) DISGAS generates 2D matrices written in GRD-format for the gas concentration, each corresponding to a different Z-layer (e.g. c_00i_00000j.grd where i denotes the layer and j the time slice). Moreover, disgas can produce GRD files containing the x and y components of the wind velocity at each Z-layer (e.g. u_00i_0000j.grd where i denotes the layer and j the time slice).

The output files are stored in the directory defined by the *OUTPUT_DIRECTORY* record of the DIS-GAS control file. Files in GRD format can be read by several plotting programs like the commercial software Surfer.

B.8 The problemname.log file

The name of this file is passed with the program call argument. It contains information concerning the run (summary of input data, run time error messages, CPU time, *etc.*).

B.9 The restart file restart.dat

The restart file is automatically produced by **disgas** and is overwritten at each print step. This file contains all the information needed to restart the simulation starting from the time of last dump. This may be usefull for long runs that need to be interrupted and then restart, or for modifying some parameters (*e.g.* the wind field or the source file) during runtime. The restart file is written in binary and cannot be directly edited. The format of the restart file is defined in the subroutines **wrirst.f90** (which generates the restart file), both located in the directory **src**.

Appendix C Format of the GRD files

The GRD files follow the Golden Surfer structure, as described in Table 4. The meaning of the used symbols is the following:

- ID : Four-characters identification string. The string DSAA identifies an ASCII grid file, whereas the string DSBB identifies a BINARY file.
- NX : Number of grid points along x-direction
- NY : Number of grid points along *y*-direction
- XMIN : x-coordinate of the grid left corners
- XMAX : x-coordinate of the grid right corners
- YMIN : y-coordinate of the grid bottom corners
- YMAX : y-coordinate of the grid top corners
- ZMIN : Minimum value in the grid
- ZMAX : Maximum value in the grid
- MAT : Matrix values at each grid point. It consists of an array of NX×NY values organized in row order. The pixels start from the bottom-left corner and move right along the row. Rows are written from bottom to top. Last value refers to the top-right corner.

In the BINARY files NX and NY are INTEGER(2), XMIN, XMAX, YMIN, YMAX, ZMIN and ZMAX are REAL(8), and the valuers of MAT are REAL(4).

```
DISGAS INPUT FILE
TTME.
  YEAR = 2007
  MONTH = 2
  DAY
        = 24
  HOUR = 12
  MINUTE = 00
  SIMULATION_INTERVAL_(SEC) = 120
  RESTART_RUN = NO
  RESET_TIME = NO
GRID
  NX
        = 40
  NY
        = 32
  NZ
        = 11
  Z_LAYERS_(M) = 0. 1. 4. 8. 12. 16. 24. 32. 40. 50. 60.
  DX_{(M)} = 50.
  DY_(M) = 50.
  X_ORIGIN_(UTM_M) = 427000
  Y_ORIGIN_(UTM_M) = 4520000
PROPERTIES
  DISPERSION_TYPE = PARTICLES
                                     (GAS/PARTICLES)
   PARTICLE_DIAMETER = 2.0e-6
                                     (PARTICLE DIAMETER IN M)
   PARTICLE_DENSITY = 2610.
                                     (PARTICLE DENSITY KG/M3)
   PARTICLE_SHAPE_PARAMETER=0.779
                                    (PARTICLE SPHERICITY)
   PARTICLE_MODEL_VSET = GANSER
                                    (ARASTOOPOUR/GANSER/WILSON_HUANG)
TOPOGRAPHY
  EXTRACT_TOPOGRAPHY_FROM_FILE = YES
                                        (YES/NO)
  Z_ORIGIN_(M) = 0.0
  X_SLOPE_(DEG) = 0.0
  Y_SLOPE_(DEG) = 0.0
METEO
  WIND_MODEL
                       = DIAGNO
                                        (SIMILARITY/DIAGNO)
  HORIZONTAL_TURB_MODEL = SMAGORINSKY
                                        (CONSTANT/SMAGORINSKY)
  VERTICAL_TURB_MODEL = SIMILARITY
                                        (CONSTANT/SIMILARITY)
  ROUGHNESS_MODEL = UNIFORM
                                        (UNIFORM/MATRIX)
  ROUGHNESS_LENGTH
                      = 0.18
                                        (Roughness length if UNIFORM)
  DIFF_COEFF_HORIZONTAL = 10.
                                        (Only for turbulence model=0)
  DIFF_COEFF_VERTICAL = 10.
                                        (Only for turbulence model=0)
 FILES
                                        (Relative or absolute file paths)
   TOPOGRAPHY_FILE_PATH = topography.grd
   ROUGHNESS_FILE_PATH = roughness.grd
   RESTART_FILE_PATH
                        = restart.dat
                       = source.dat
   SOURCE_FILE_PATH
   WIND_FILE_PATH
                       = winds.dat
                       = diagno.out
   DIAGNO_FILE_PATH
   OUTPUT_DIRECTORY
                       = outfiles
OUTPUT
 LOG_VERBOSITY_LEVEL = 0
                                          (0/1)
  OUTPUT_GRD_TYPE
                      = ASCII
                                          (ASCII/BINARY)
  OUTPUT_INTERVAL_(SEC) = 21600
                                          (Number of seconds between prints)
  OUTPUT_U_VELOCITY = NO
                                          (YES/NO)
  OUTPUT_V_VELOCITY = NO
                                          (YES/NO)
  OUTPUT_W_VELOCITY = NO
                                          (YES/NO)
  OUTPUT_CONCENTRATION = YES
                                          (YES/NO)
  OUTPUT_LAYERS = ALL
                                          (ALL/List_of_layers)
  TRACK_POINTS = NO
                                          (YES/NO)
  N_POINTS = 2
                                          (Number of tracking points)
  POINTS\_EASTING = 643080 641000
                                          (UTM easting coordinate of each tracking point)
  POINTS_NORTHING = 1774150 1774250
                                          (UTM northing coordinate of each tracking point)
  POINTS_ELEVATION = 1 1
                                          (Meters above ground of each tracking point)
```

Table 1: Sample of the input control file problemname.inp

X_UTM iyr t_1	Y_UTM imo t_2	Zref idy wx	ihr wy	imi T_z0	code T_zref	# code=CUP p
t_(nt-1)	t_nt	wx	wy	T_z0	T_zref	р

Table 2: Format of the wind file winds.dat with code=CUP.

Table 3: Format of the wind file winds.dat with code=SONIC.

X_UTM iyr t_1	Y_UTM imo t_2	Zref idy wx	ihr wy	imi T_zref	code ustar	# code=SONIC L
		wx				
t_(nt-1)	t_nt		wy	T_zref	ustar	L

Table 4: Format of a GRD file

ID			
NX NY			
XMIN XMAX			
YMIN YMAX			
MIN(VAL) M	IAX (V	AL)	
VAL(i,1)		• • •	i=1:NX
	• • •	• • •	
VAL(i,j)	• • •	•••	i=1:NX
•••	• • •	•••	
VAL(i,NY)	• • •	• • •	i=1:NX

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